

**III**

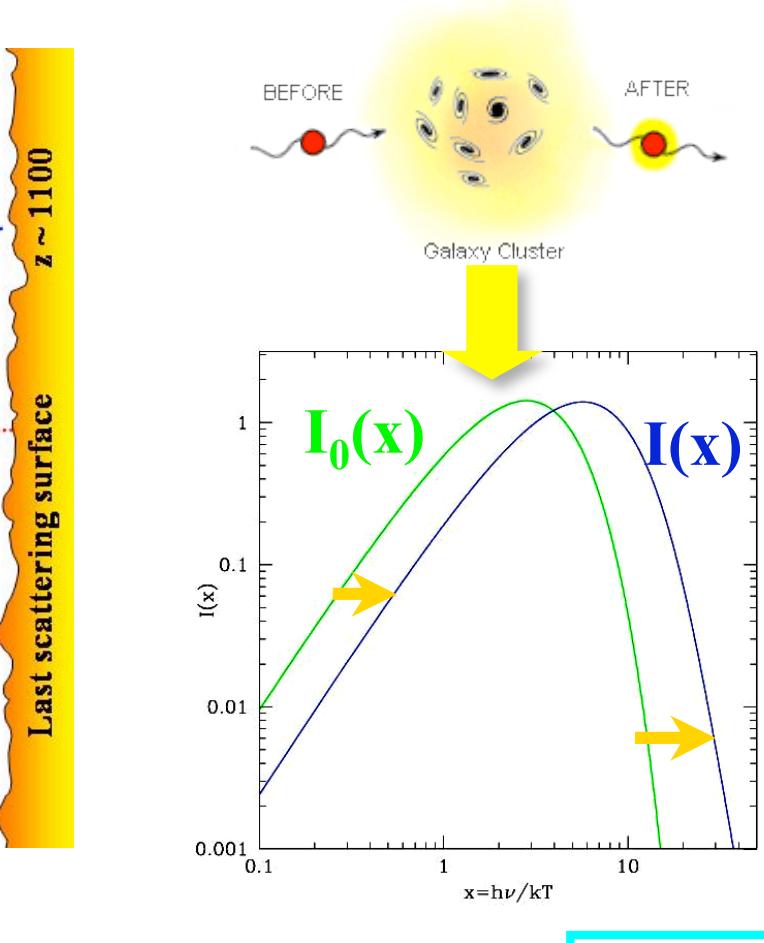
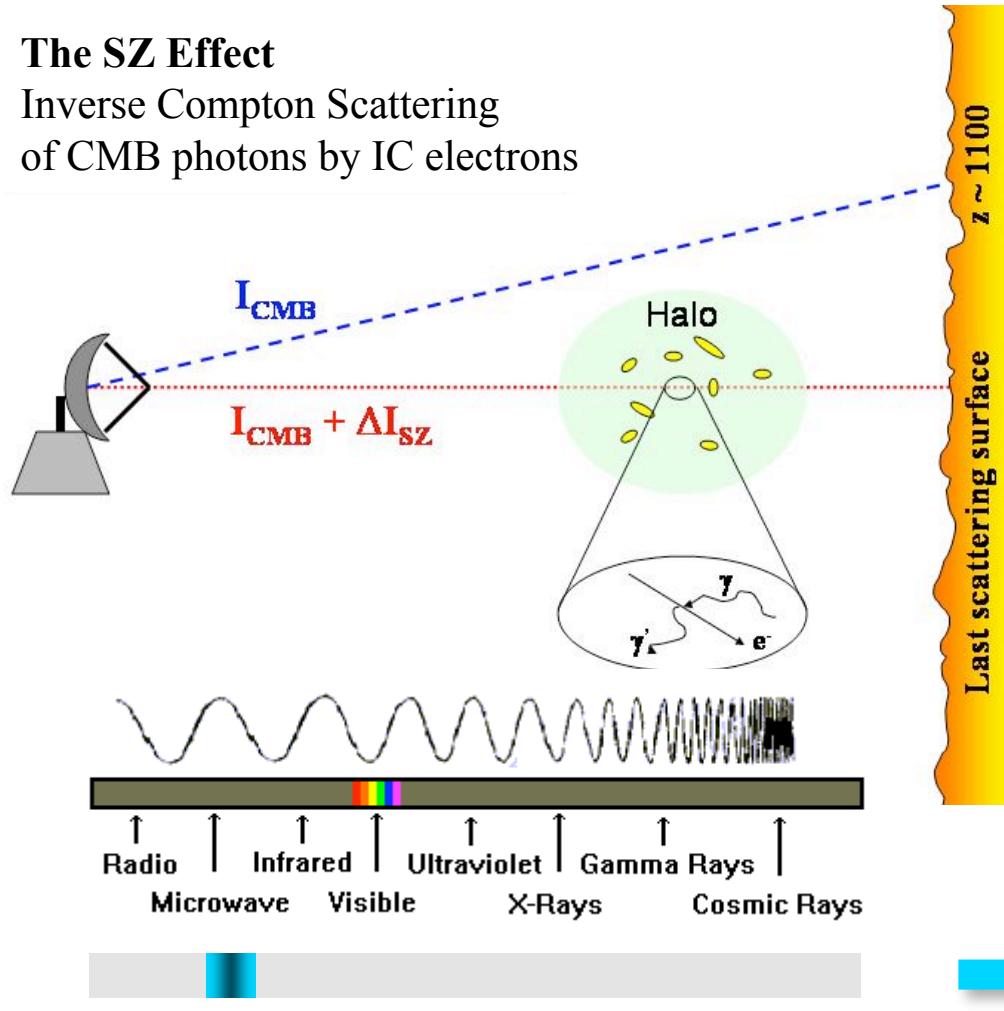
# **SZ effects with ALMA**

Credit: S. Colafrancesco

# SZ effect: the standard lore

## The SZ Effect

Inverse Compton Scattering  
of CMB photons by IC electrons



thermal, non-rel.  $e^-$

$$\frac{\Delta\nu}{\nu} \approx 4 \frac{kT_e}{m_e c^2}$$

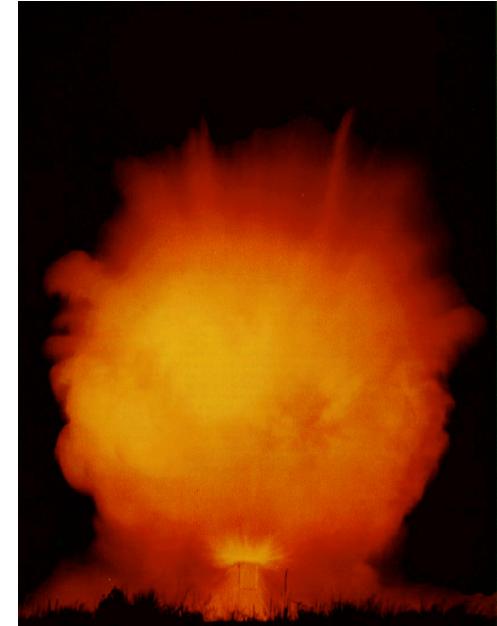
# The origin of the SZ effect

## Non-coherent Compton Scattering

Fall-out effect of the Cold War

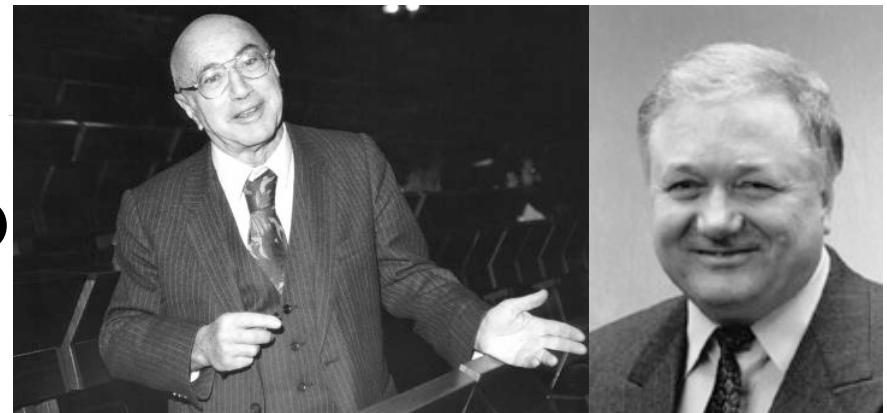
1957 A.S. Kompaneets publishes his  
Compton scattering Fokker-Planck  
equation

$$\frac{\partial n}{\partial y} = \frac{1}{x^2} \frac{\partial}{\partial x} x^4 \left( \frac{\partial n}{\partial x} + n + n^2 \right)$$

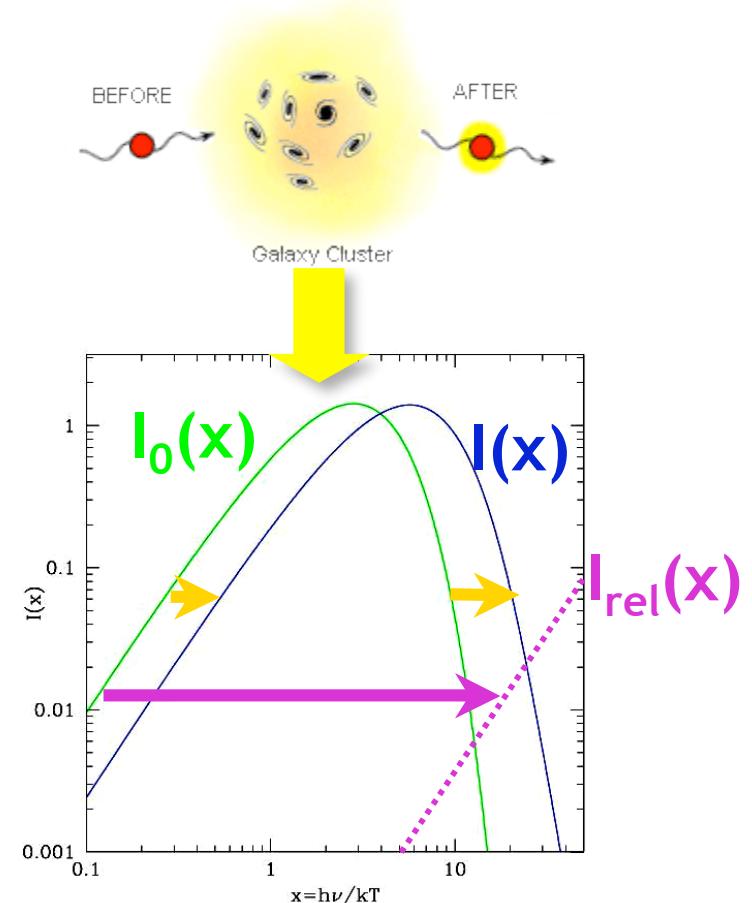
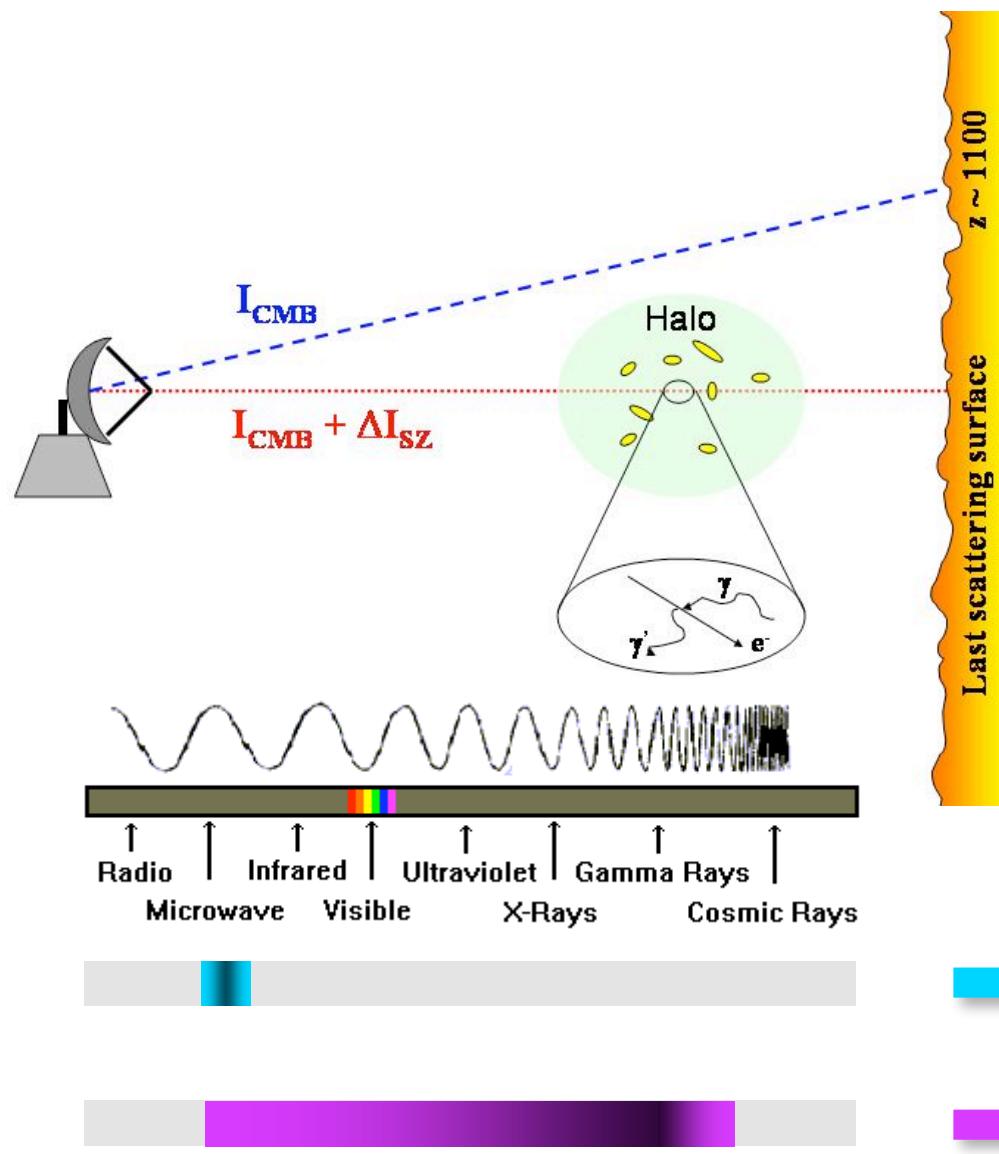


(derived by A.S. Kompaneets in Soviet Union ~1950  
but was classified due to bomb research until 1956)

1969 Ya. B. Zel'dovich & R. Sunyaev  
derive the SZ effect  
(i.e., applied the Kompaneets eq.  
for a thermal intracluster plasma)



# SZ effect: ...more than basics



thermal NR  $e^-$

$$\frac{\Delta\nu}{\nu} \approx 4 \frac{kT_e}{m_e c^2}$$

relativistic  $e^-$

$$\frac{\Delta\nu}{\nu} \approx \frac{4}{3} \gamma^2$$

# SZE: general derivation

Intensity change

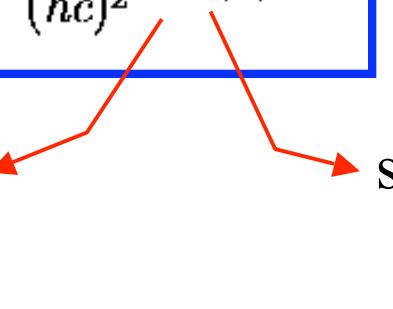
$$\Delta I(x) = 2 \frac{(k_B T_0)^3}{(hc)^2} y \tilde{g}(x)$$

$$y = \frac{\sigma_T}{m_e c^2} \int P d\ell.$$

electron “Pressure”

in thermal case

$$P_{th} = n_e k_B T_e \rightarrow \text{Mass}$$



spectral shape

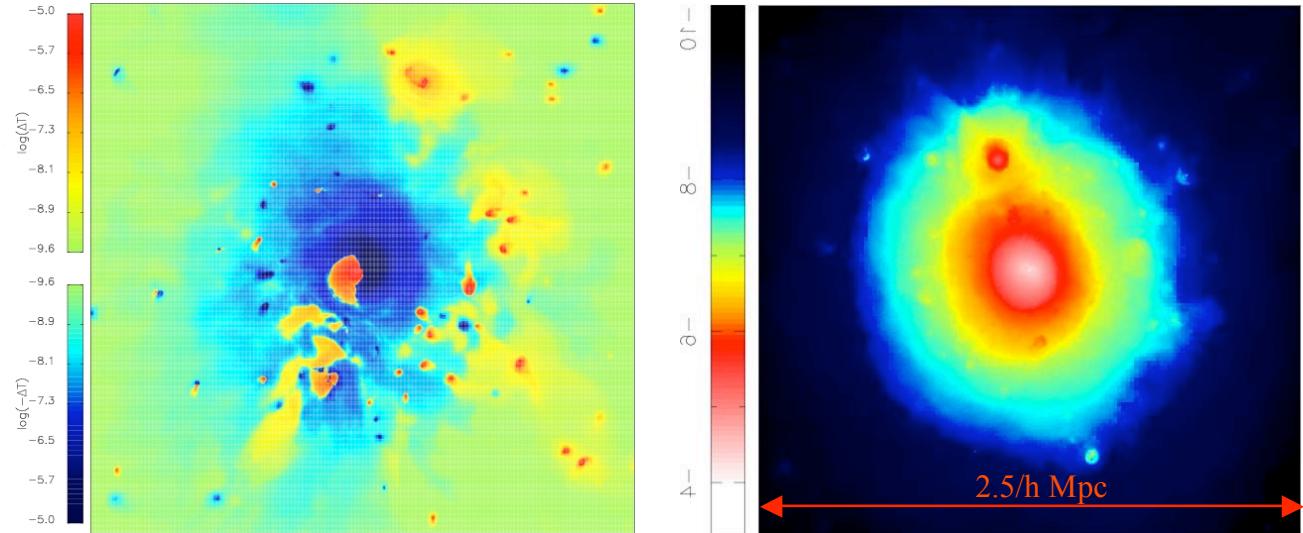
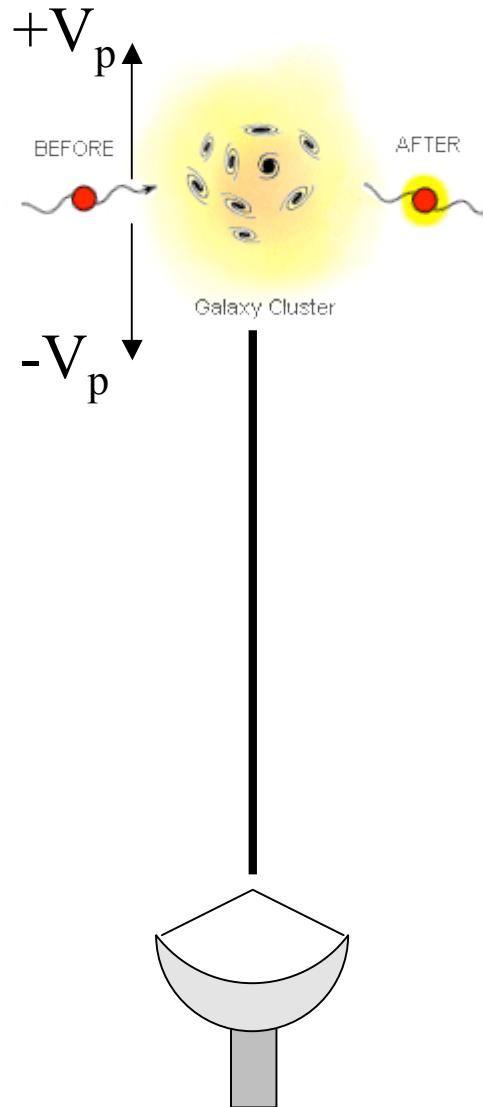
depends on electrons  
energy distribution

Note: **redshift not involved**  $\Rightarrow$  detectability independent of redshift  
(provided that the angular resolution is appropriate)

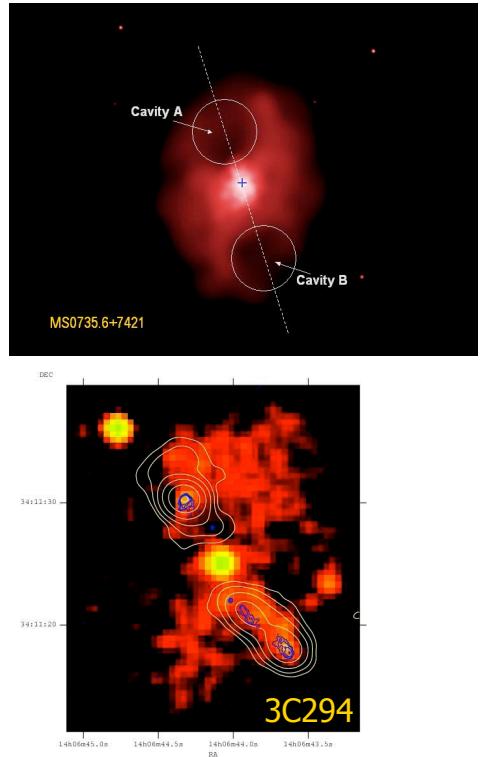
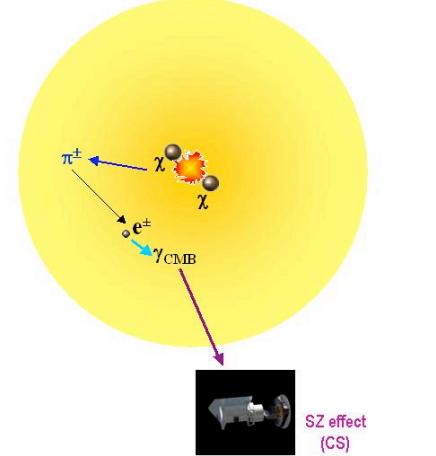
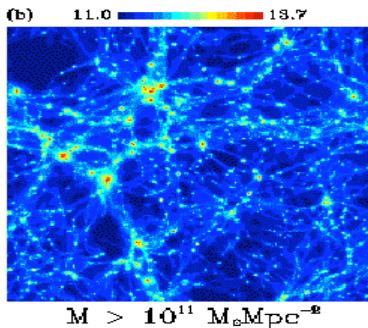
# SZE: other sources

Kinematic SZE

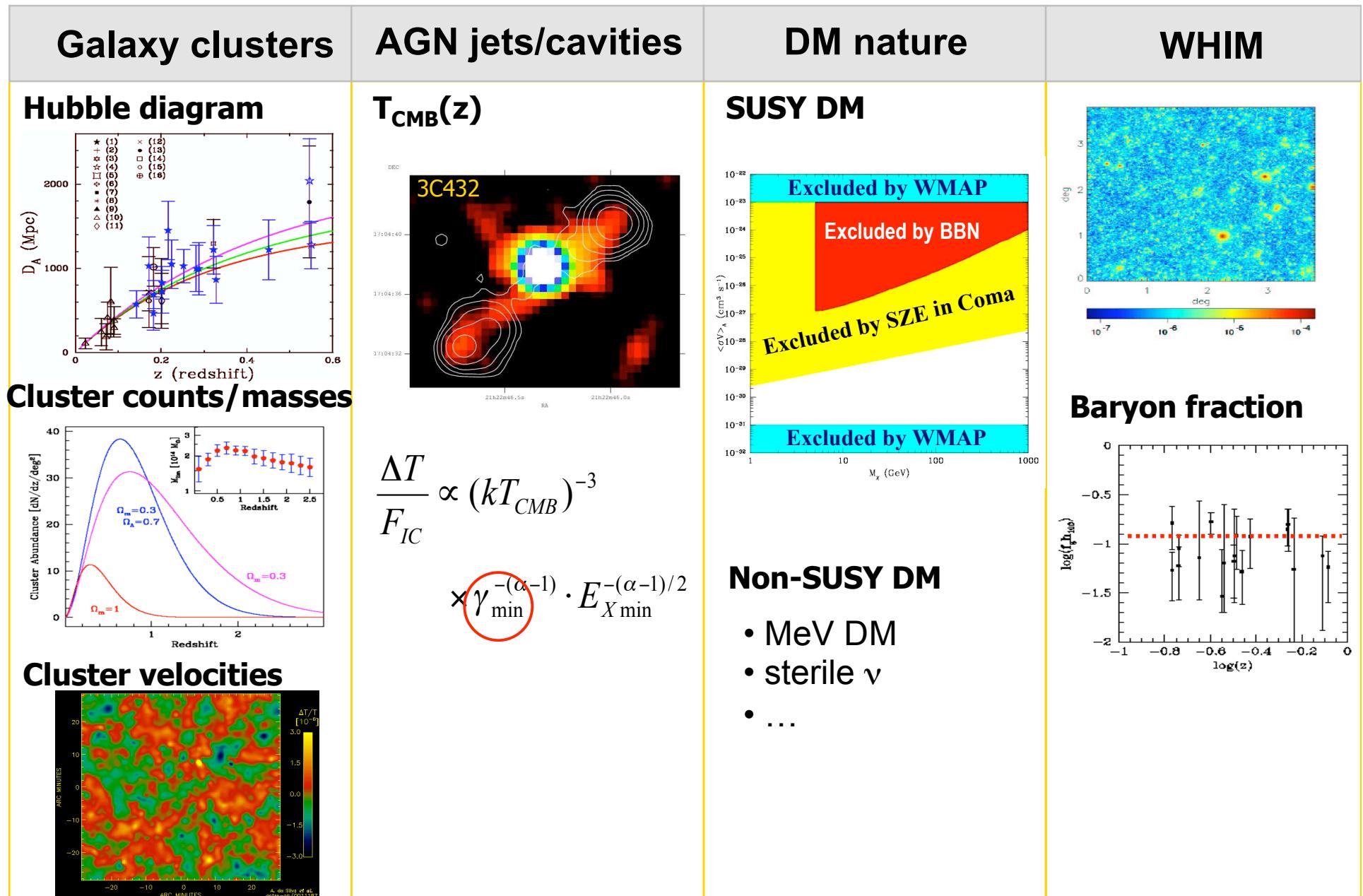
$$\frac{\Delta T}{T} = \frac{\pm V_p}{c} \tau$$



# Sources of SZ

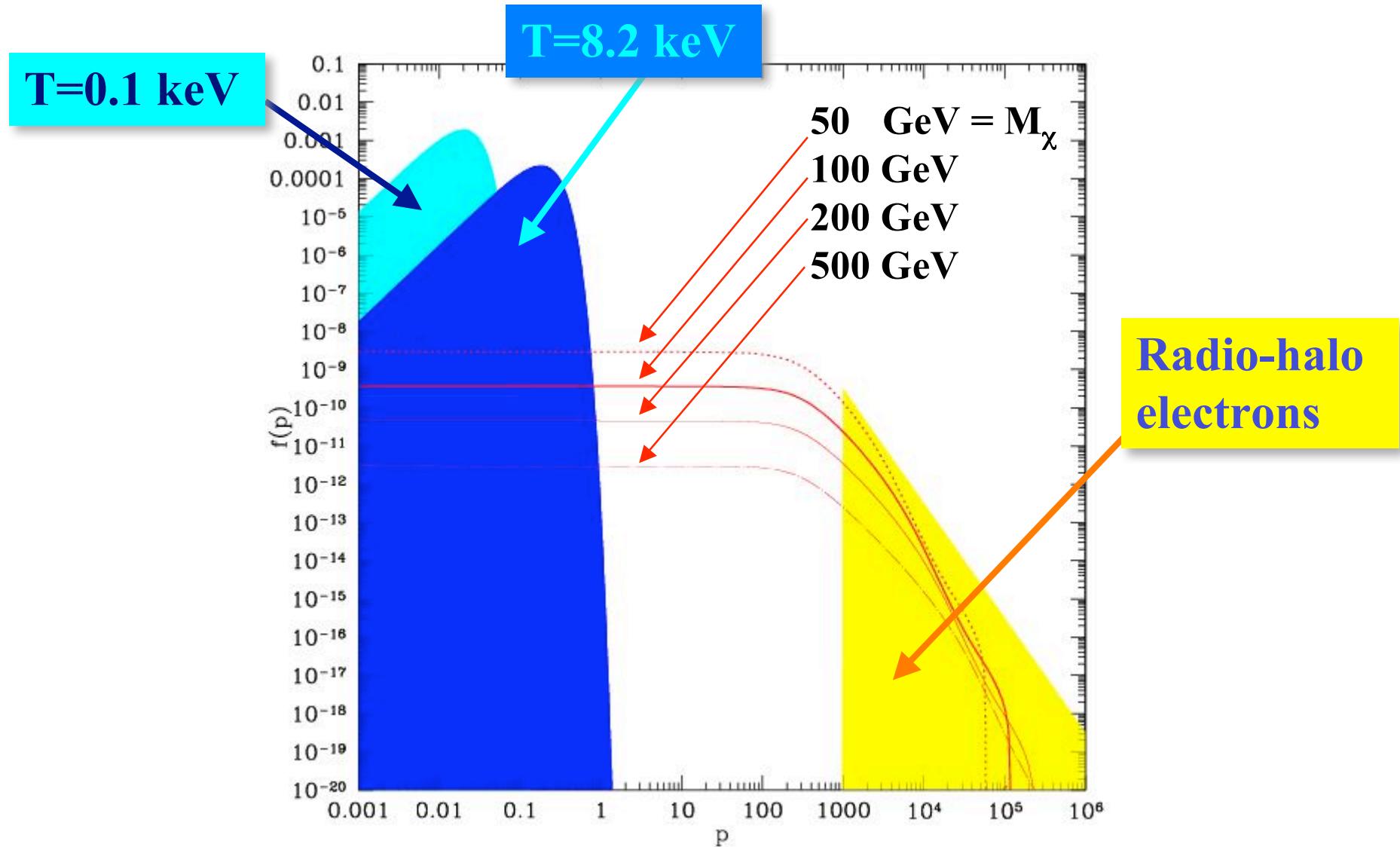
Galaxy clusters	AGN jets/cavities	Dark Matter	WHIM
	 <p>MS0735.6+7421</p> <p>3C294</p>	 <p><math>\pi^+</math></p> <p><math>e^+</math></p> <p><math>\gamma_{\text{CMB}}</math></p> <p>SZ effect (CS)</p>	 <p>(b)</p> <p>11.0 18.7</p> <p><math>M &gt; 10^{11} M_e \text{Mpc}^{-3}</math></p>

# Astrophysical relevance



# The $e^\pm$ distribution in clusters

**COMA:** warm gas + hot gas + radio halo + DM halo

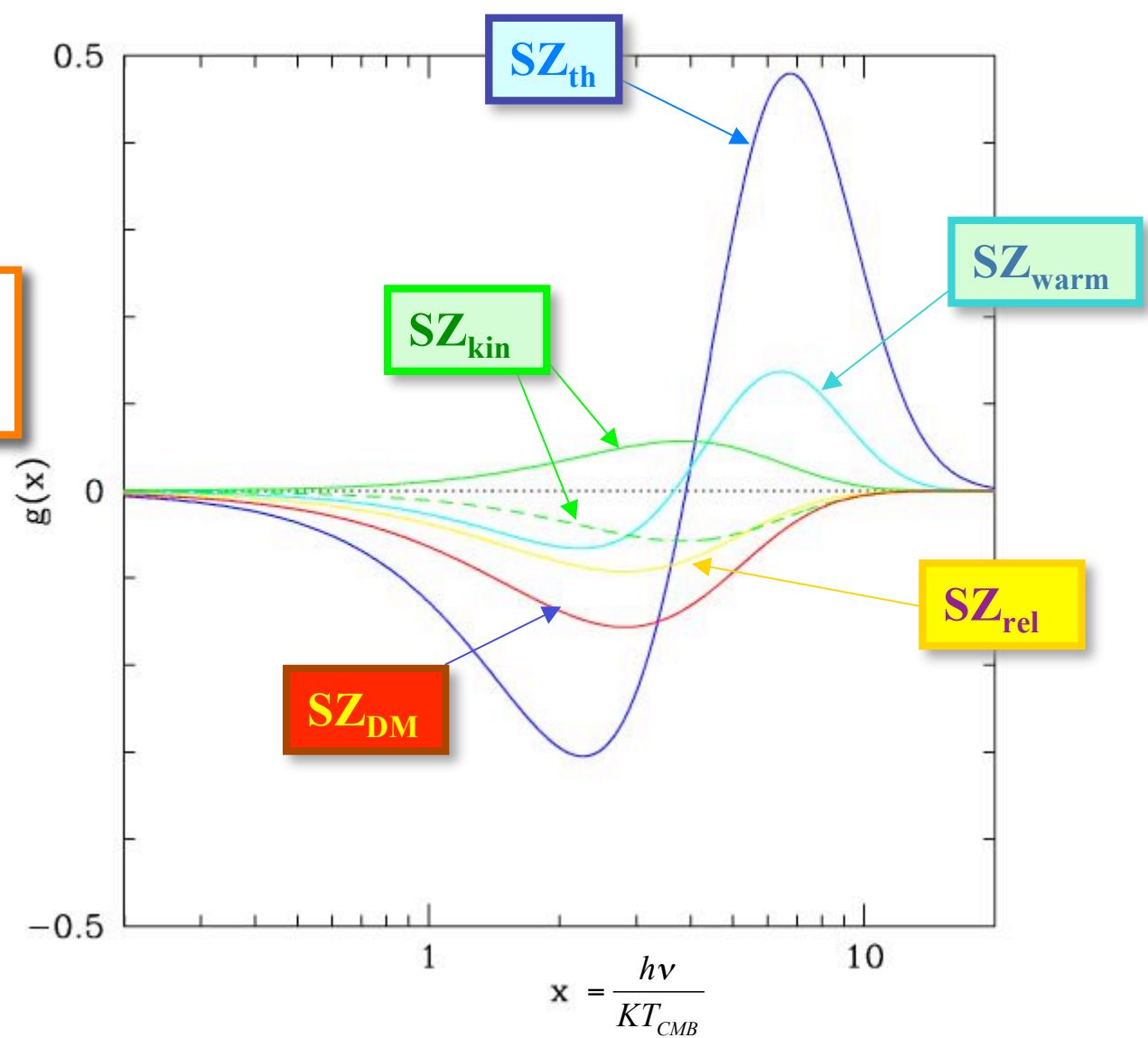


# The SZE from various $e^\pm$ pops.

Colafrancesco 2007

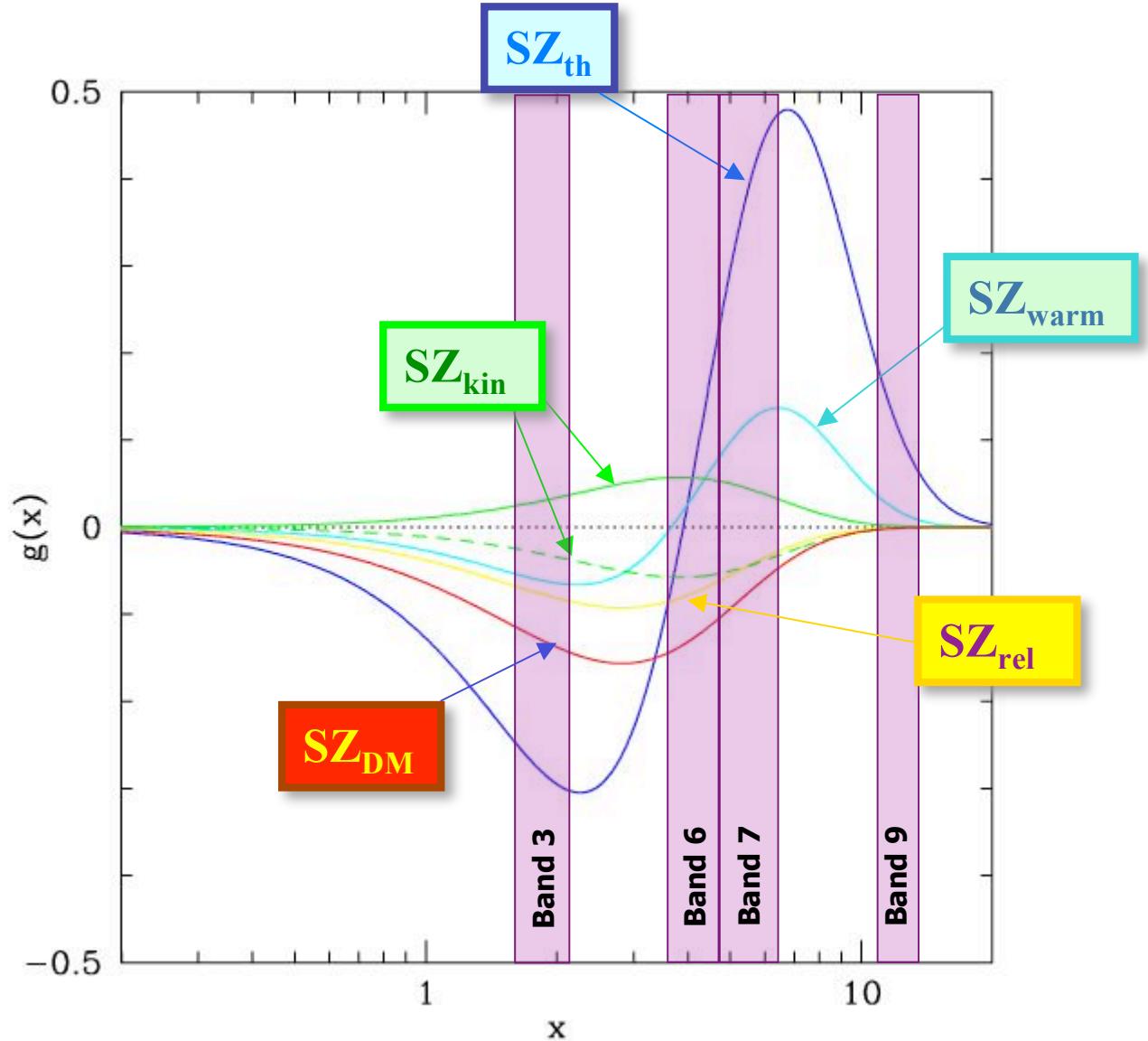
$$\Delta I(x) = 2 \frac{(k_B T_0)^3}{(hc)^2} y \tilde{g}(x)$$

$$y = \frac{\sigma_T}{m_e c^2} \int P d\ell.$$

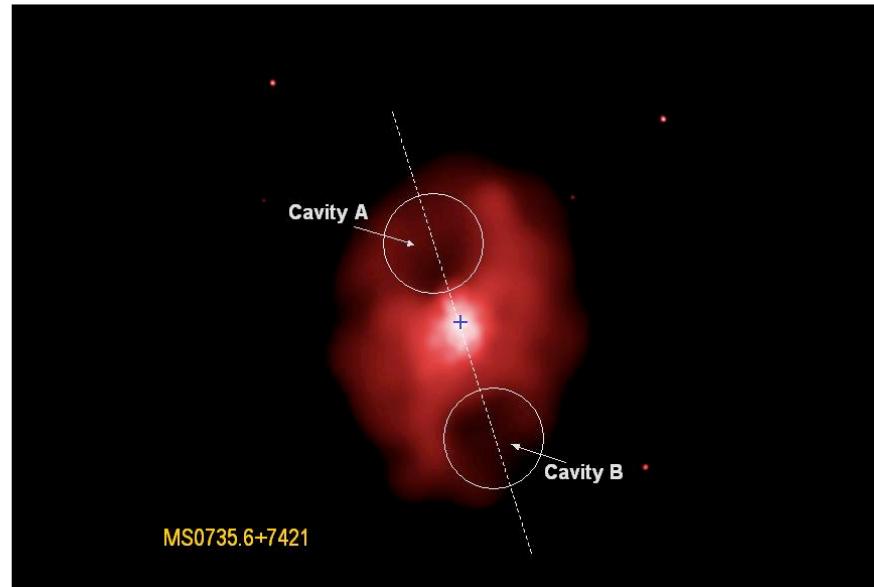
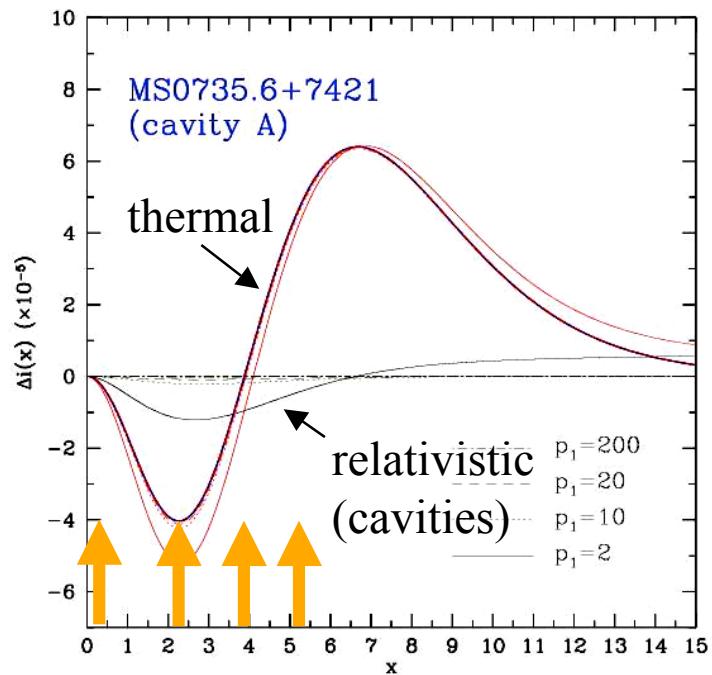


# SZE: ALMA $\nu$ -coverage

ALMA reference $\nu$ -bands	
<b>Band 3</b>	86 – 116 GHz
<b>Band 6</b>	211 – 275 GHz
<b>Band 7</b>	275 – 370 GHz
<b>Band 9</b>	602 – 720 GHz



# SZE & cavities in clusters

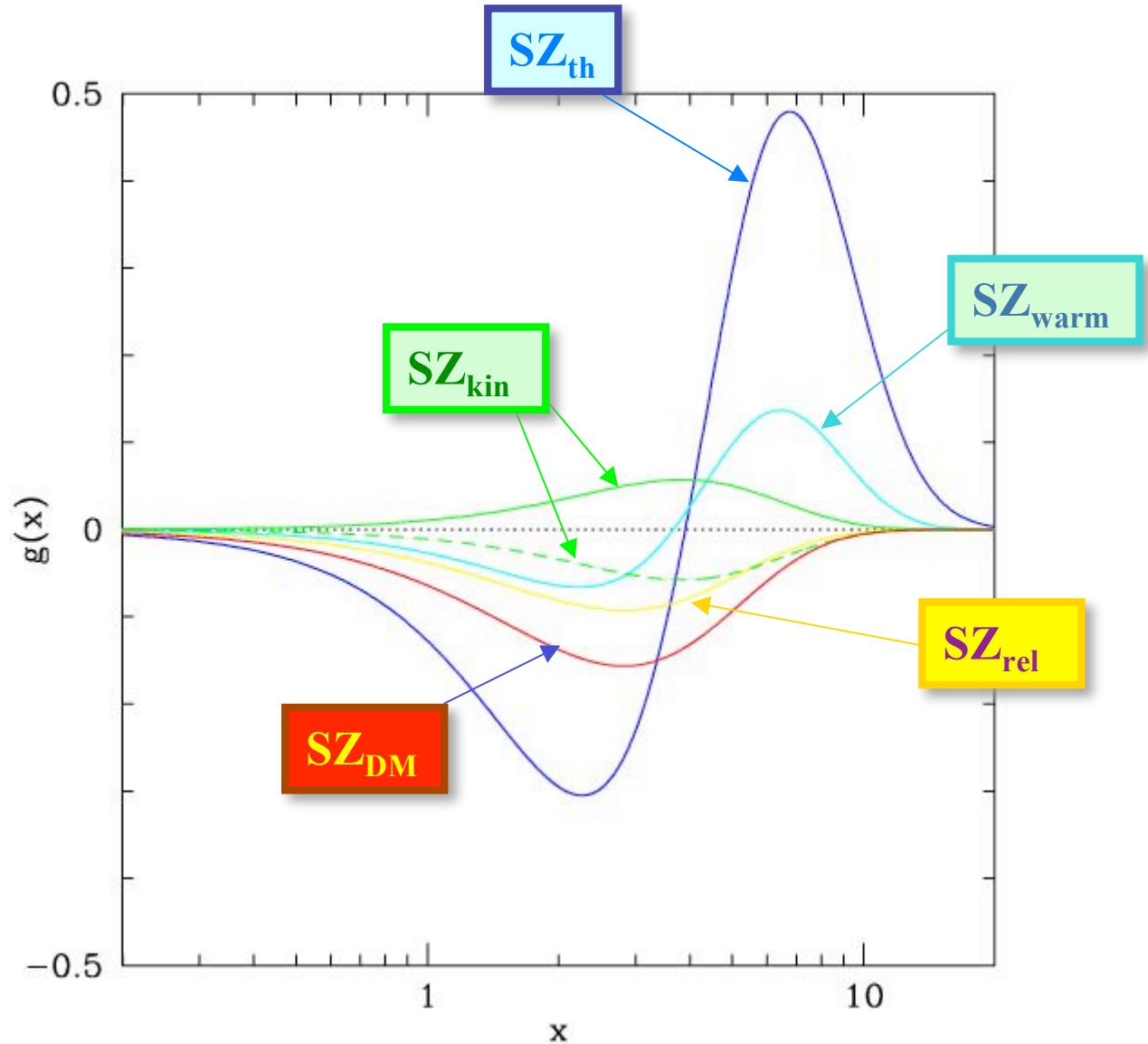


Colafrancesco+05

# SZE in DM halos

A structure with:

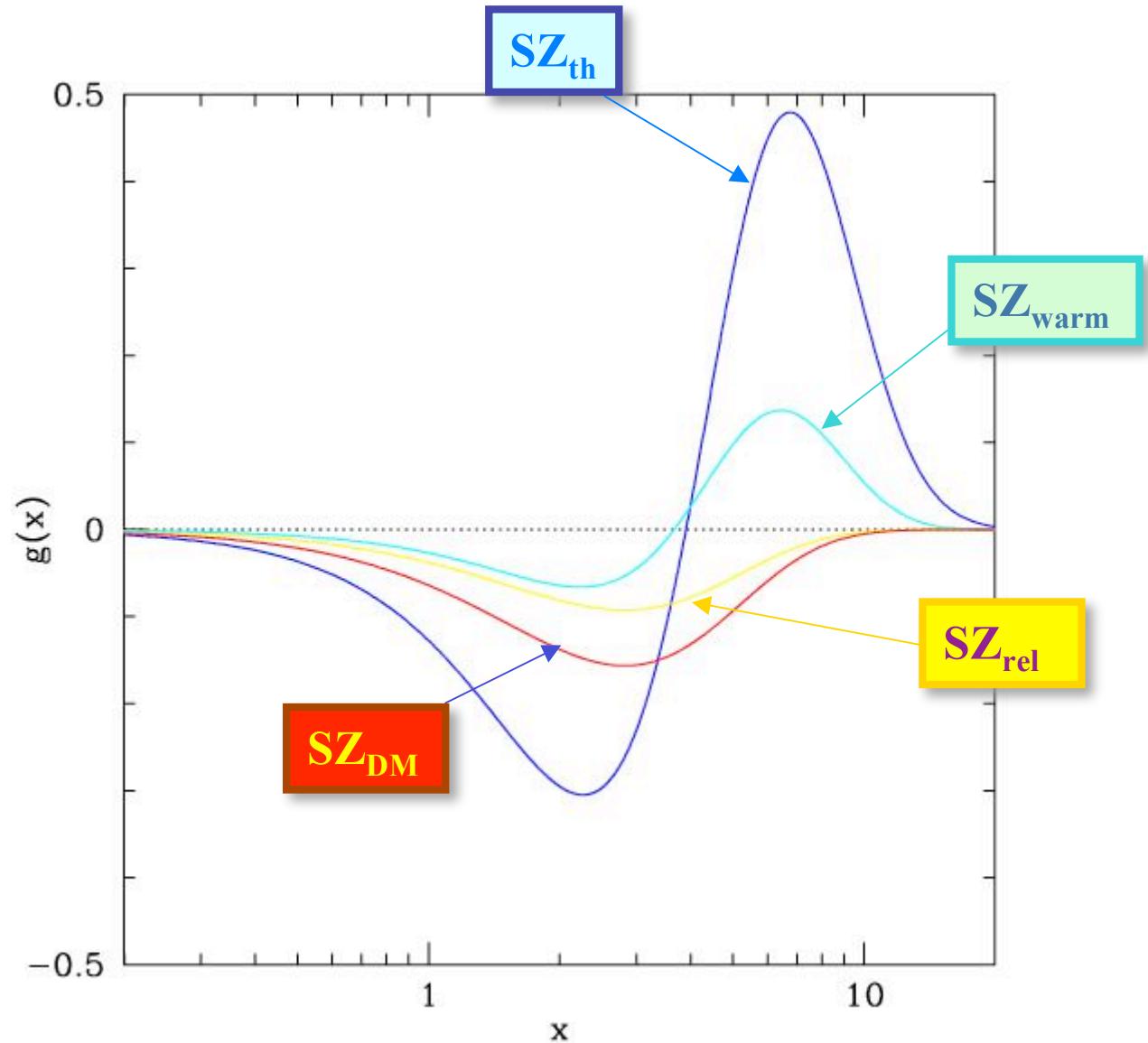
- Hot gas
- Warm gas
- Rel. Plasma
- DM
- Distant &  $V_r$



# SZE in DM halos

A structure with:

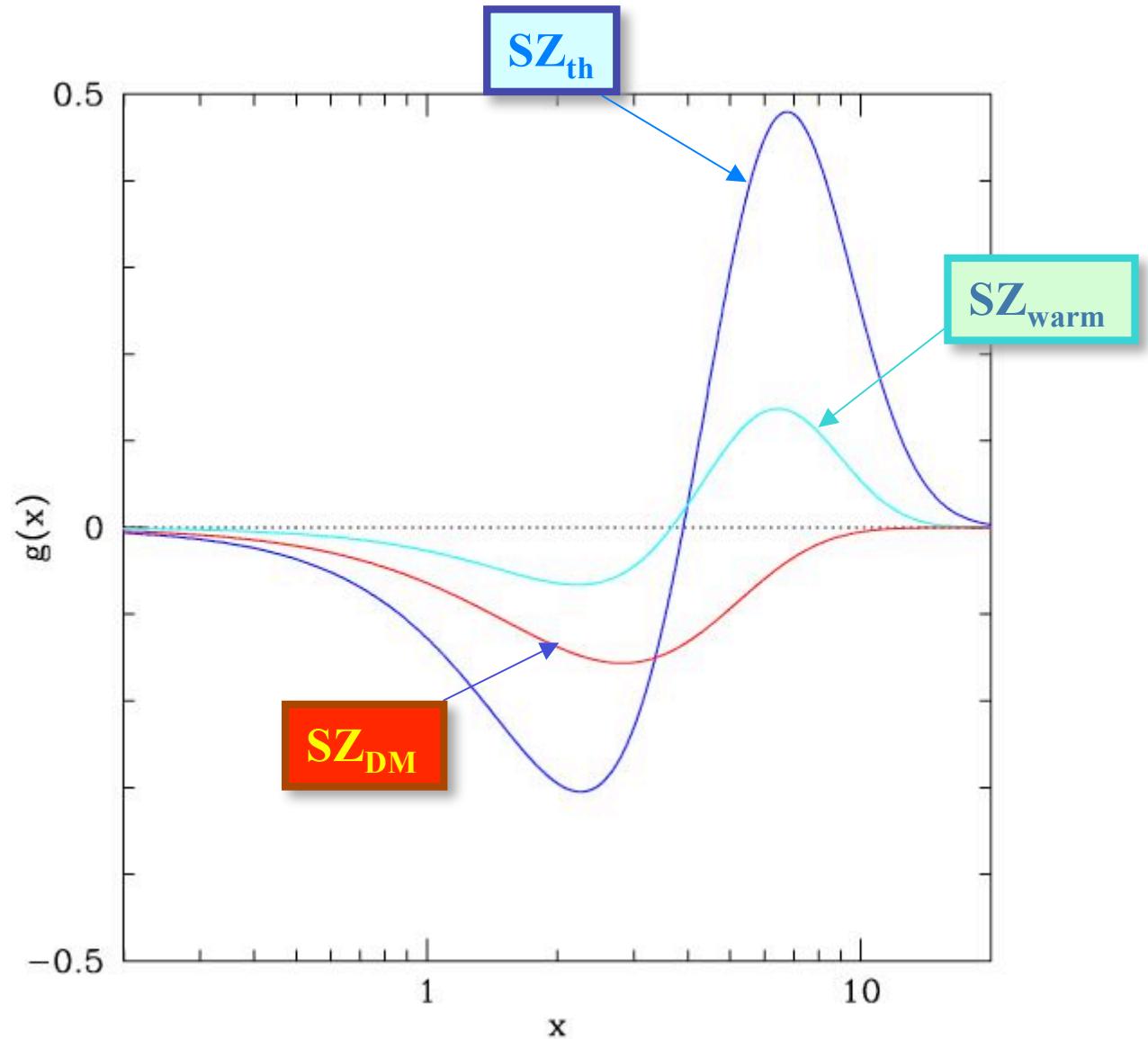
- Hot gas
- Warm gas
- Rel. Plasma
- DM
- Nearby ( $V_r \approx 0$ )



# SZE in DM halos

A structure with:

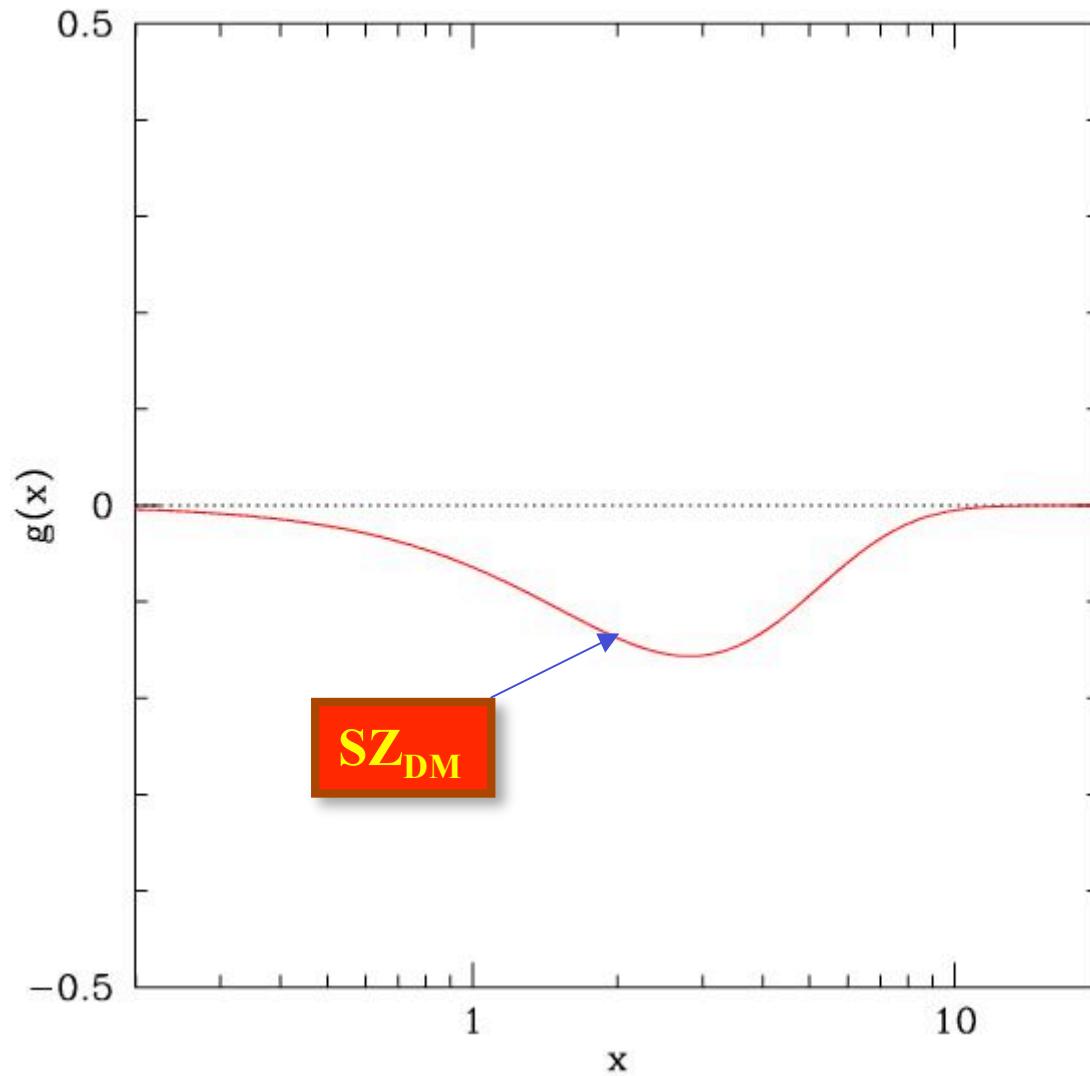
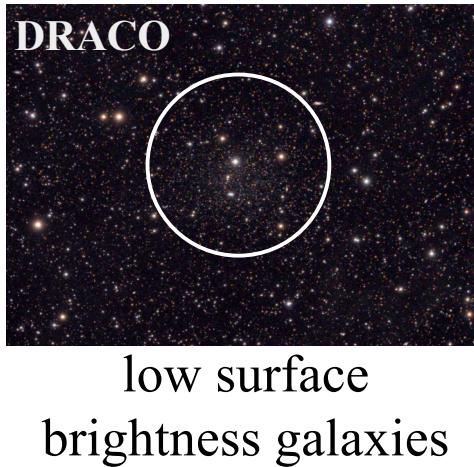
- Hot gas
- Warm gas
- DM
- Nearby ( $V_r \approx 0$ )



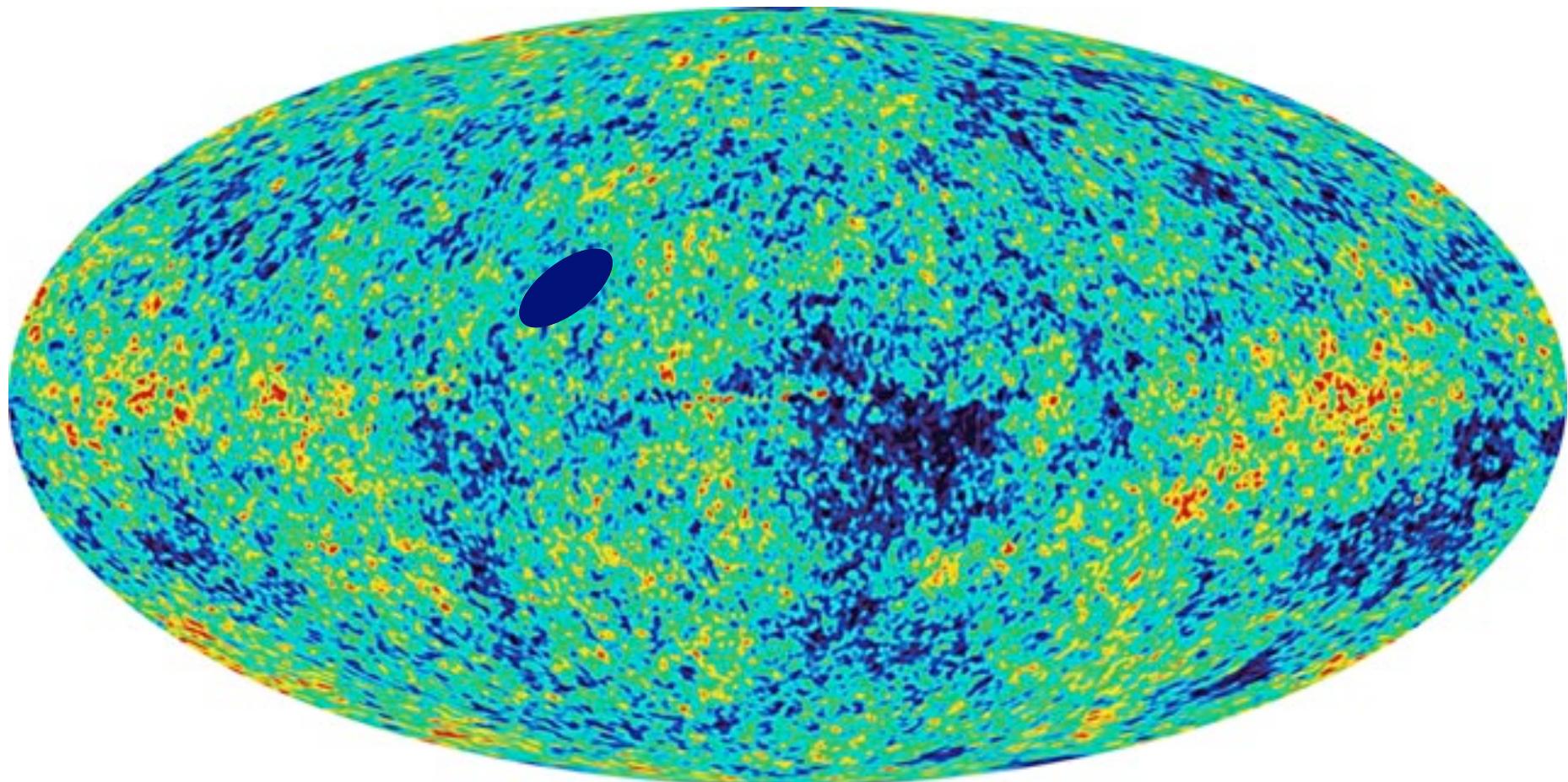
# SZE in DM halos

A structure with:

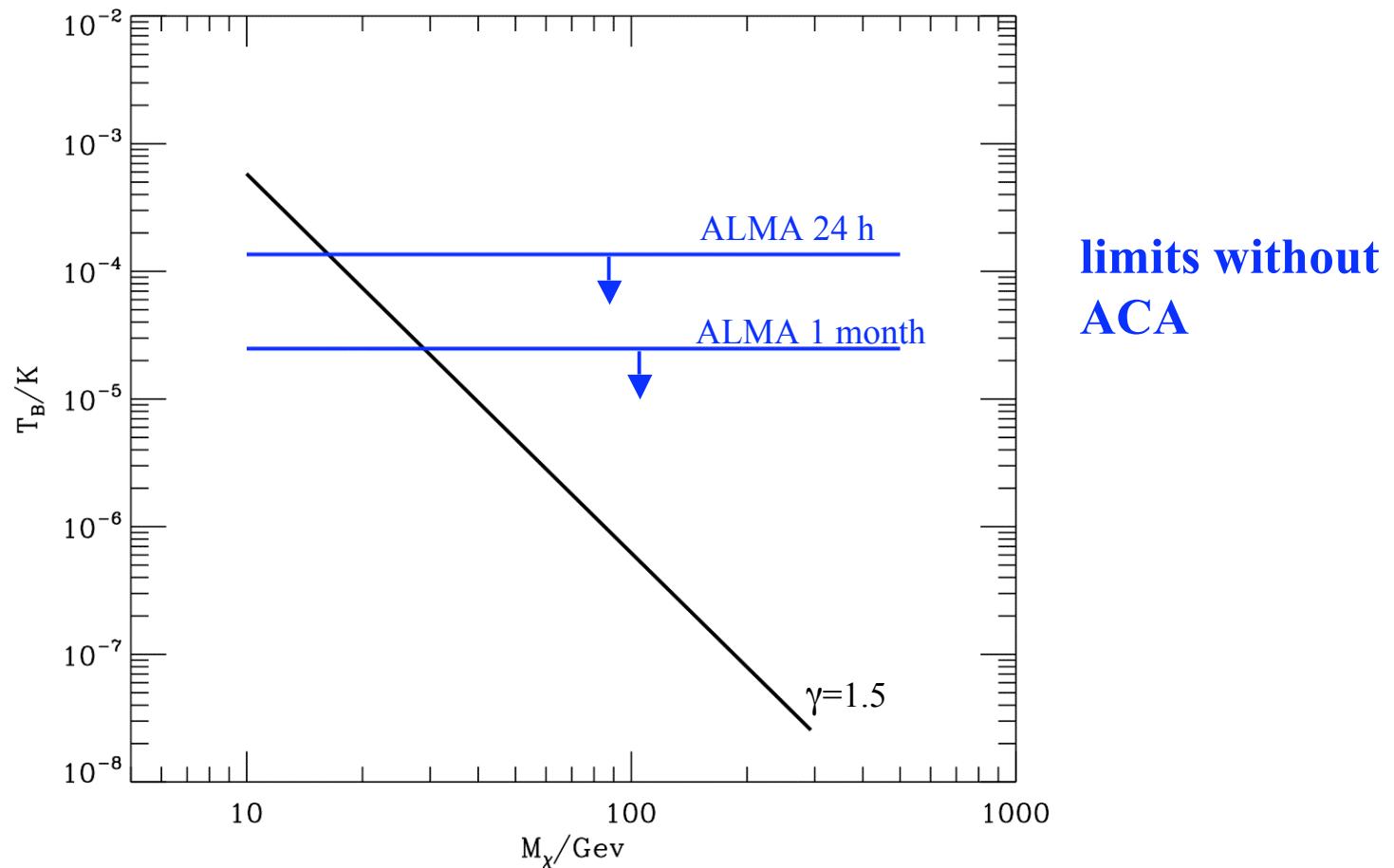
- Blue
- Cyan
- Yellow
- **DM**
- **Nearby ( $V_r \approx 0$ )**



# CMB maps & DRACO

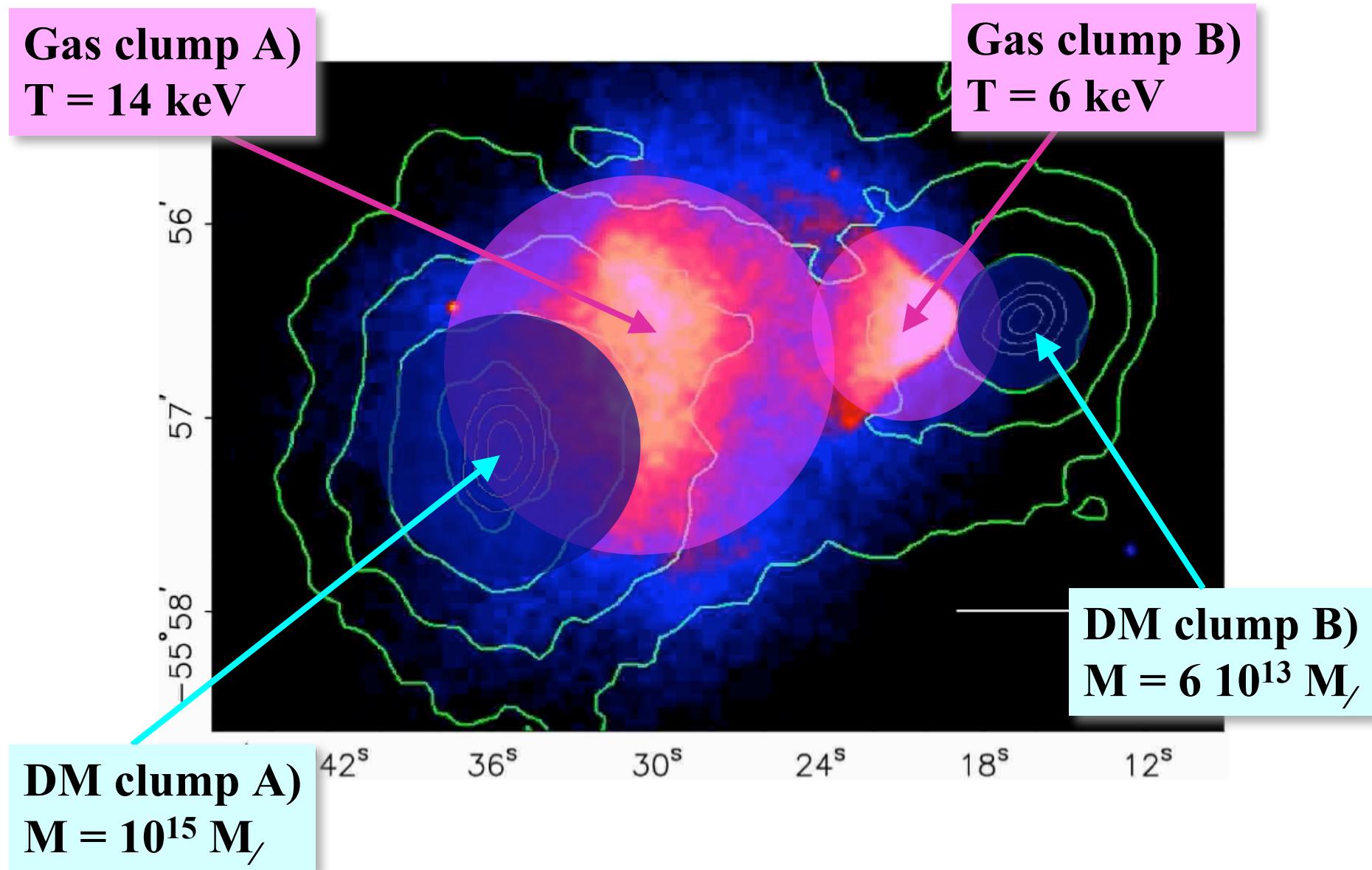


# SZ<sub>DM</sub> in Draco

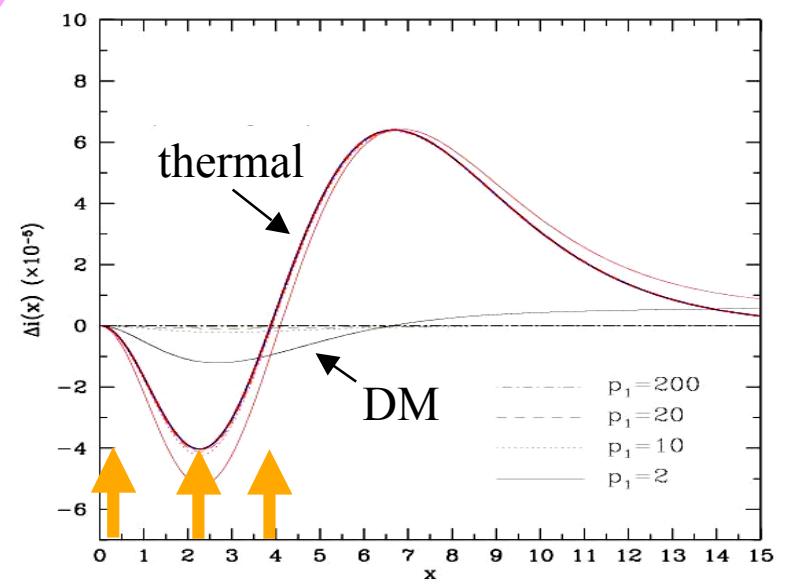
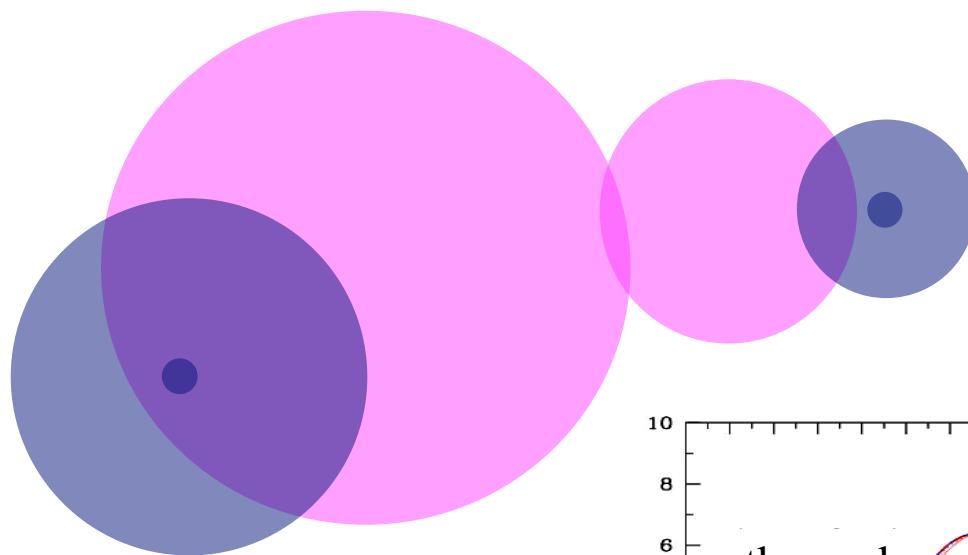


adapted from Culverhouse+06

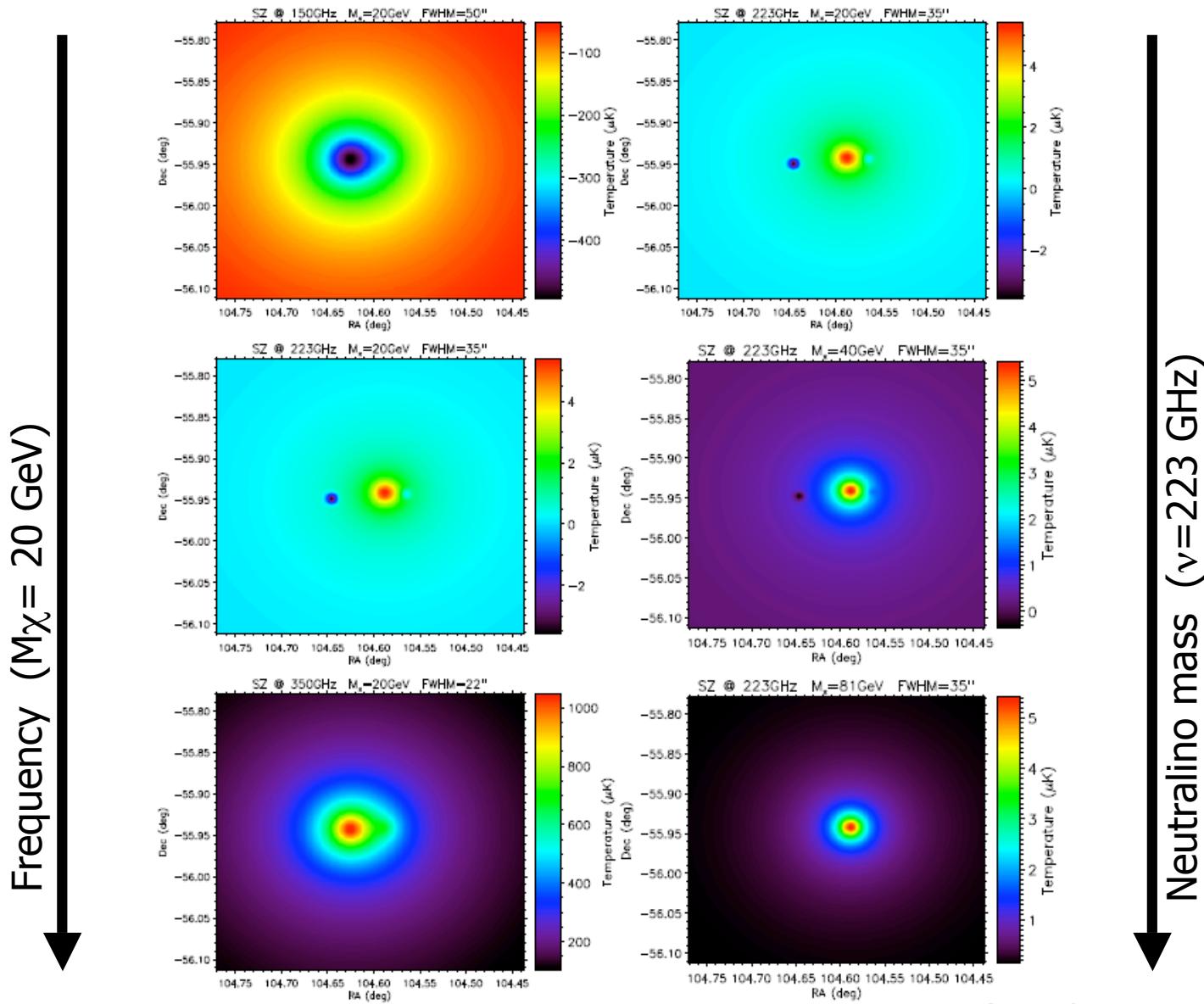
# The cluster 1ES0657-556



# The SZ<sub>DM</sub> from 1ES0657-556

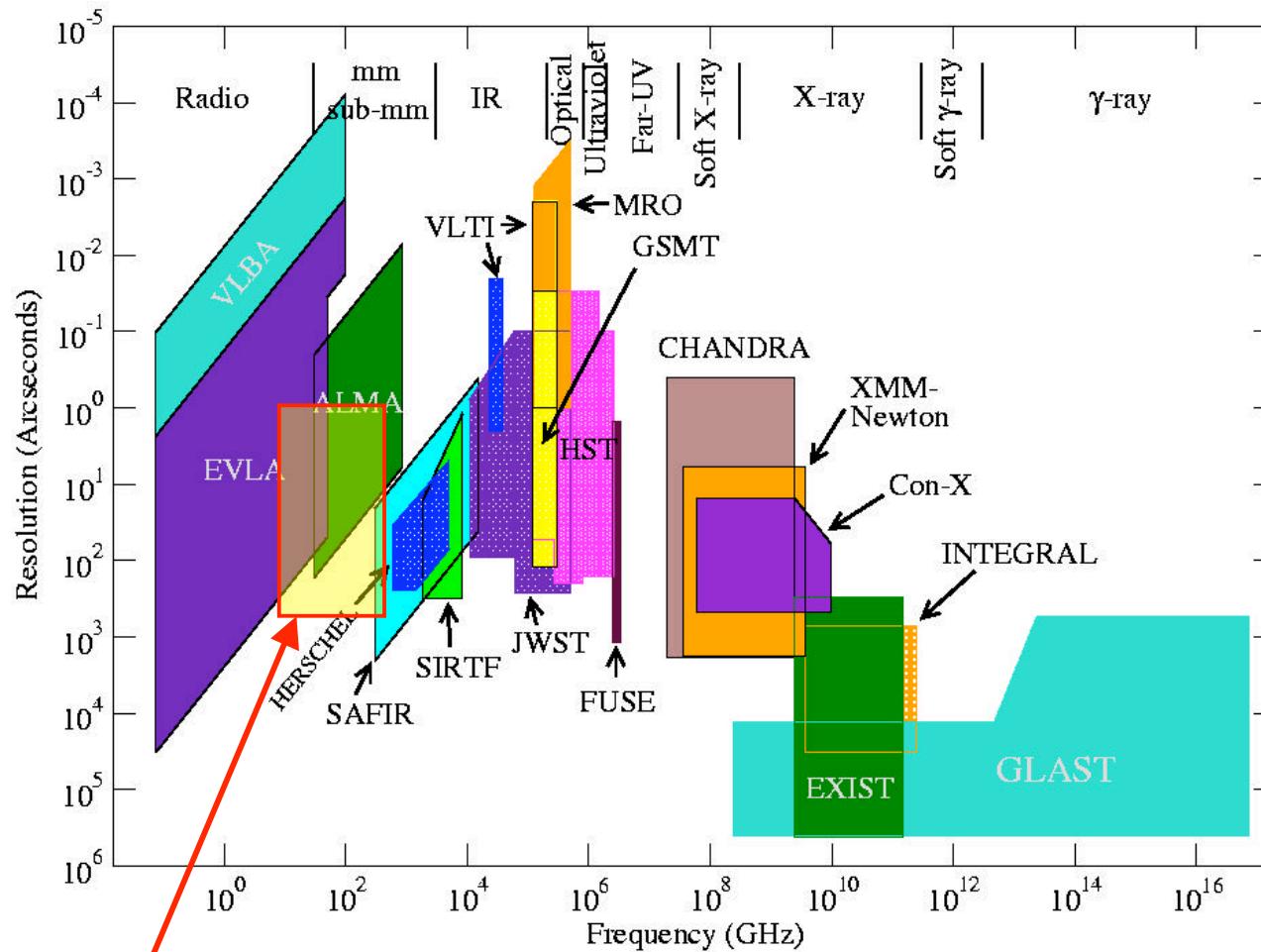


# Isolating SZ<sub>DM</sub> at ~223 GHz



Colafrancesco+07

# SZE science: requirements



**SZE**

**Resolution:  $1'' - 10'$**

**$\Delta\nu = 10 - 500 \text{ GHz}$**